



第二章:

大气环流的外部强迫(II) -Simple energy balance climate model 授课教师:张洋

2023.10.19





第二章:

大气环流的外部强迫(II)

Reference reading: Lindzen 2005, Chapter 2

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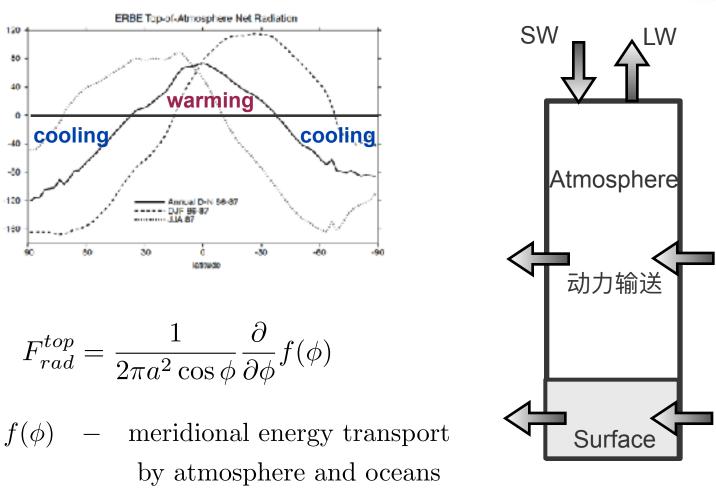
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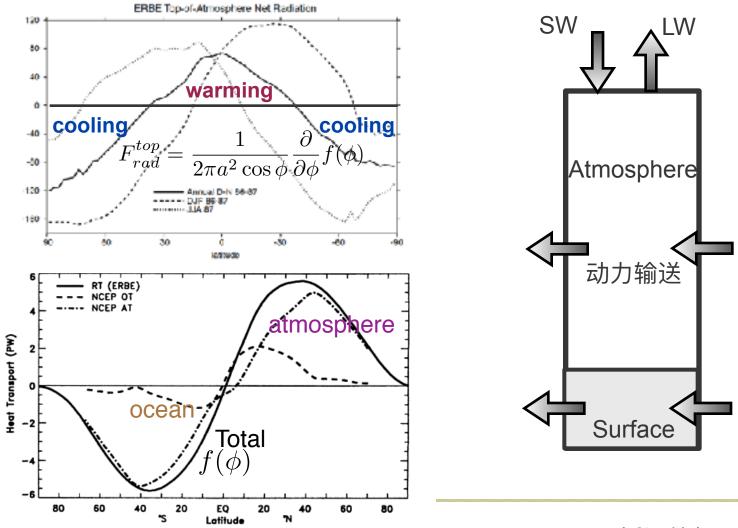
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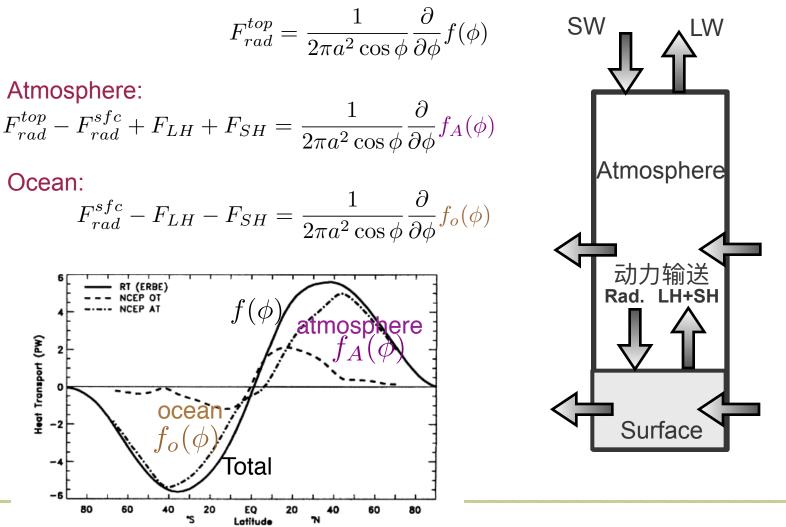




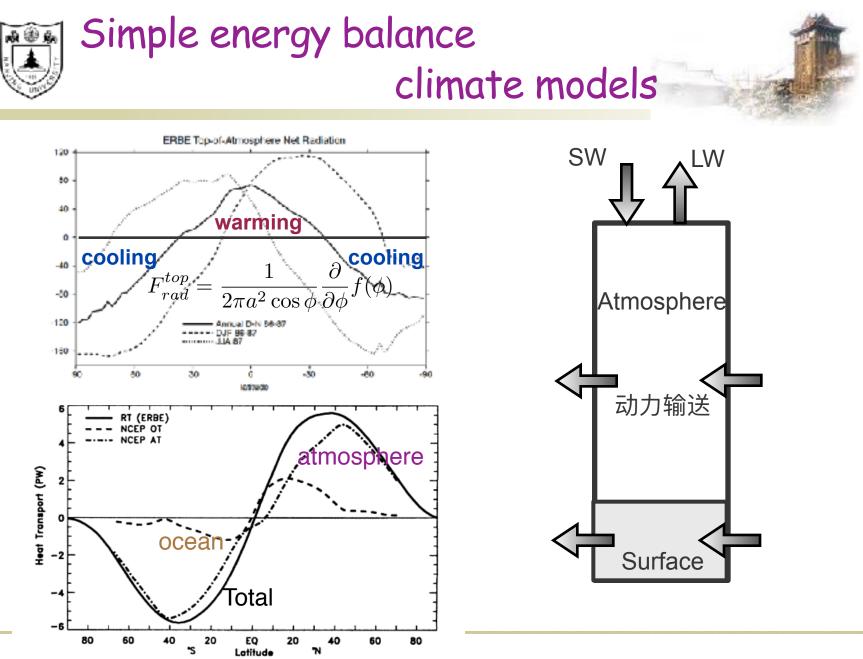
Wunsch (2005), J. Climate







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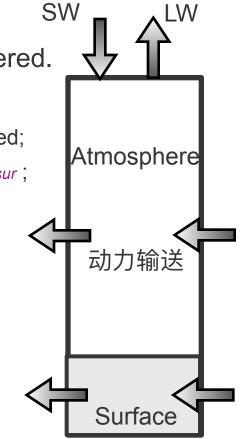
Simple energy balance climate models

- Simplest models in which the interactions between ^S *radiation* and *dynamic heat transport* can be considered.
 - Assumptions are made below:
 - One-dimensional, only latitude dependences are considered;
 - Global energy budgets are assumed to be expressed in *T_{sur}*;
 - Only annual mean conditions are considered;

 $\mathcal{C}\frac{\partial T(x,t)}{\partial t} = \text{solar radiation} - \text{infrared cooling} \\ -\text{divergence of heat flux}$

 $x = \sin \phi$, where ϕ is latitude.

$$C\frac{\partial T(x,t)}{\partial t} = F_{rad}^{top} - \frac{1}{2\pi a^2}\frac{\partial}{\partial x}f(x)$$





solar radiation – infrared cooling
–divergence of heat flux

 $x = \sin \phi$, where ϕ is latitude.

solar radiation = $Qs(x)\mathcal{A}(T)$

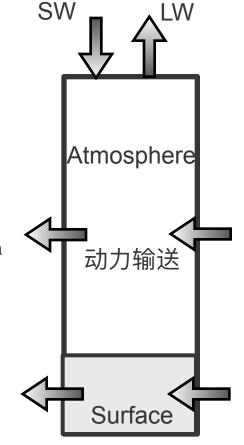
s(x) – latitudinal distribution of SW, whose integral from the equator to pole is unity

$$C\frac{\partial T(x,t)}{\partial t} = Qs(x)\mathcal{A}(T) - I(T) + F(T)$$

In equilibrium,

 $\mathcal{C}\frac{\partial T(x,t)}{\partial t}$

$$Qs(x)\mathcal{A}(T) - I(T) + F(T) = 0$$





In equilibrium,

$$Qs(x)\mathcal{A}(T) - I(T) + F(T) = 0$$

The snow line case:

- Made assumptions below:
 - Planetary albedo is assumed to depend primarily on snow /ice cover;

$$\mathcal{A}(T) = \alpha, \quad \text{for } T < T_{snow}$$

or = $\beta, \quad \text{for } T > T_{snow}$

SW

W

Atmosphere

动力输送

Surface



In equilibrium,

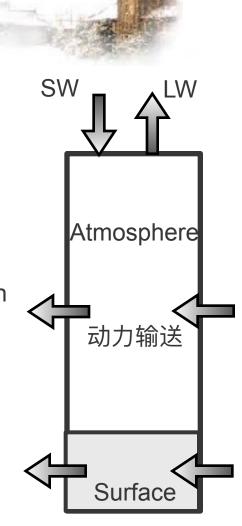
$$Qs(x)\mathcal{A}(T) - I(T) + F(T) = 0$$

The snow line case:

- Made assumptions below:
 - Planetary albedo is assumed to depend primarily on snow /ice cover;
 - The infrared cooling I = A + BT

$$\mathcal{A}(T) = \alpha, \quad \text{for } T < T_{snow}$$

or = $\beta, \quad \text{for } T > T_{snow}$





In equilibrium,

$$Qs(x)\mathcal{A}(T) - I(T) + F(T) = 0$$

The snow line case:

- Made assumptions below:
 - Planetary albedo is assumed to depend primarily on snow /ice cover;
 - The infrared cooling I = A + BT
 - The primary feature of the heat transport is that it carries heat from warmer to colder regions. $F(T) = C(\overline{T} T)$

$$A(T) = \alpha, \text{ for } T < T_{snow}$$

or $= \beta, \text{ for } T > T_{snow}$ Note: $F(T)$ is the **divergence** of heat flux

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SW

Atmosphere

动力输送

Surface



In equilibrium,

$$Qs(x)\mathcal{A}(T) - I(T) + F(T) = 0$$

- One-dimensional, only latitude dependences are considered;
- Global energy budgets are assumed to be expressed in *T_{sur}*;
- Planetary albedo is assumed to depend primarily on snow /ice cover;
- Only annual mean conditions are considered;
- The primary feature of the heat transport is that it carries heat from warmer to colder regions.

Budyko, M.I. (1969). The effect of solar radiation variations on the climate of the earth. *Tellus* **21**, 611-619.

SW

Atmosphere

动力输送

Surface



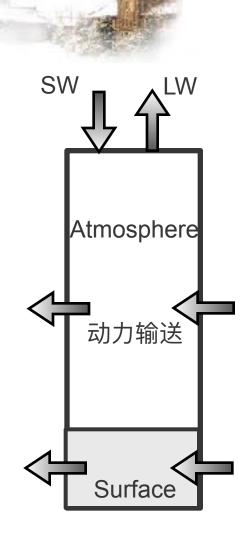
In equilibrium,

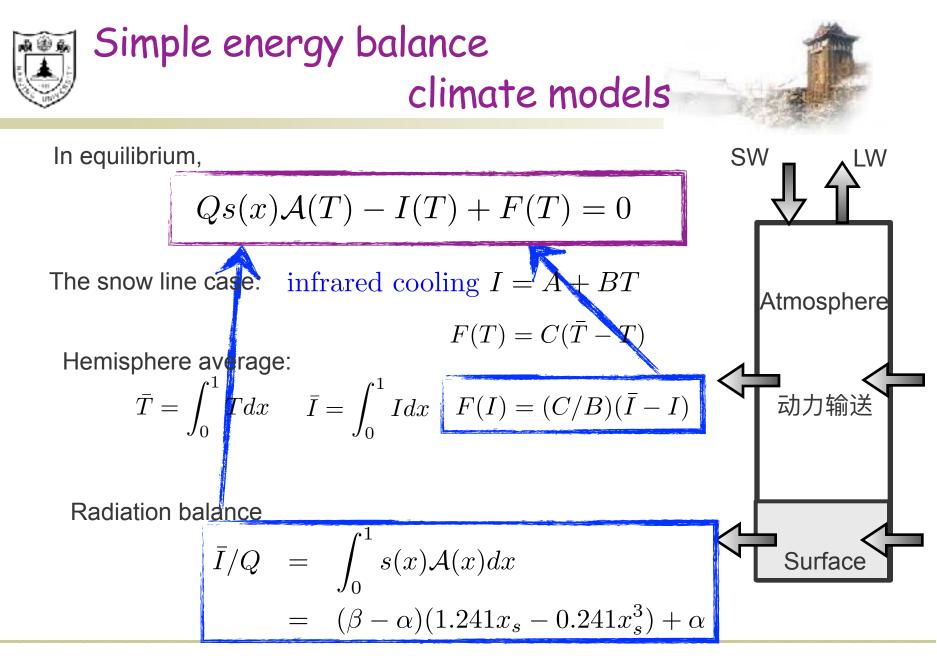
$$Qs(x)\mathcal{A}(T) - I(T) + F(T) = 0$$

The snow line case: infrared cooling I = A + BT $F(T) = C(\overline{T} - T)$

Assume:

 $\mathcal{A}(T) = \alpha = 0.4, \text{ for } T < T_{snow}$ = $\beta = 0.7, \text{ for } T > T_{snow}$ = $\frac{\alpha + \beta}{2}, \text{ for } T = T_{snow}$ $T_{snow} = -10^{\circ}C$ $s(x) = 1 - 0.241(3x^2 - 1)$ $A = 211.1 Wm^{-2}, \text{ and } B = 1.55 Wm^{-2}({}^{\circ}C)^{-1}$





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In equilibrium,

$$Qs(x)\mathcal{A}(T) - I(T) + F(T) = 0$$

The snow line case:

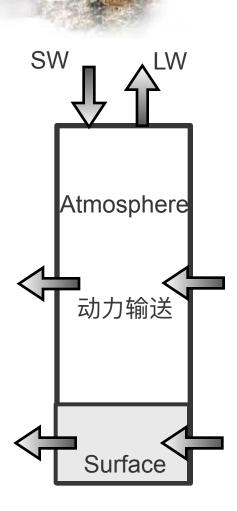
$$I/Q = \frac{\frac{C}{B}\bar{I}/Q + s(x)\mathcal{A}(x,x_s)}{1 + \frac{C}{B}}$$

Determine C using current climate:

$$I(x_s) = I(0.95) = I(T_{snow})$$
, get the value of $\frac{C}{B}$

Then

$$Q(x_s) = \frac{(1 + \frac{C}{B})(A + BT_{snow})}{\frac{C}{B}\bar{I}/Q + s(x_s)\frac{\alpha + \beta}{2}}$$

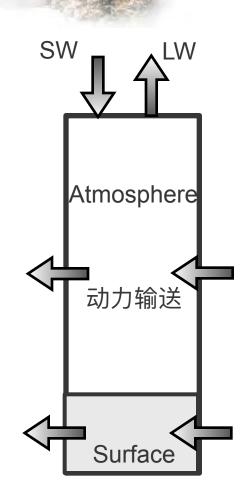


The snow line case:

$$Q(x_s) = \frac{(1 + \frac{C}{B})(A + BT_{snow})}{\frac{C}{B}\overline{I}/Q + s(x_s)\frac{\alpha + \beta}{2}}$$

The denominator:

$$den = \frac{\alpha + \beta}{2} \times 1.241 + \alpha \frac{C}{B} + \frac{C}{B} (\beta - \alpha) \times 1.241 x_s$$
$$-\frac{\alpha + \beta}{2} \times 0.723 x_s^2 - \frac{C}{B} (\beta - \alpha) \times 0.241 x_s^3$$





The snow line case:

$$Q(x_s) = \frac{\left(1 + \frac{C}{B}\right)\left(A + BT_{snow}\right)}{\frac{C}{B}\bar{I}/Q + s(x_s)\frac{\alpha + \beta}{2}}$$

If C=0, no heat flux, radiative equilibrium, then as x_s increases, den. decreases, Q increases.

太阳辐射越强,冰雪线越向两极移动

If C is nonzero,

$$den = \frac{\alpha + \beta}{2} \times 1.241 + \alpha \frac{C}{B} + \frac{C}{R}(\beta - \alpha) \times 1.241x_s$$
$$-\frac{\alpha + \beta}{2} \times 0.723x_s^2$$
$$n \text{ as } \mathbf{x}_s - \frac{C}{B}(\beta - \alpha) \times 0.241x_s^3$$



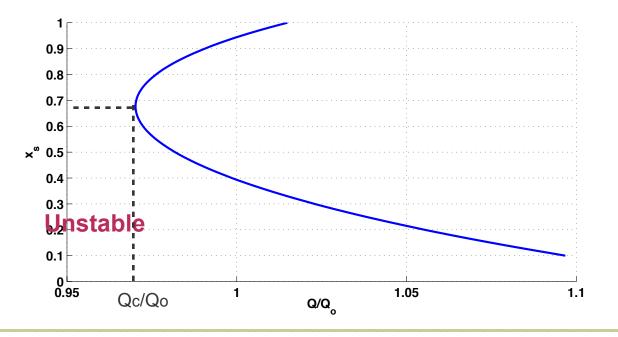
The snow line case:

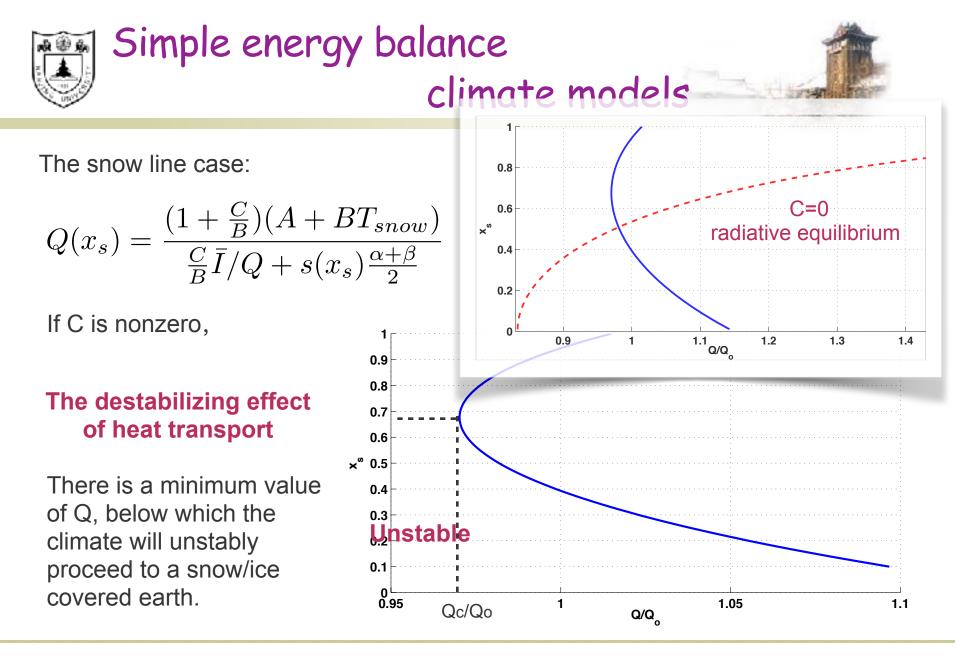
$$Q(x_s) = \frac{\left(1 + \frac{C}{B}\right)\left(A + BT_{snow}\right)}{\frac{C}{B}\bar{I}/Q + s(x_s)\frac{\alpha + \beta}{2}}$$

If C is nonzero,

The destabilizing effect of heat transport

There is a minimum value of Q, below which the climate will unstably proceed to a snow/ice covered earth.





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请在握目一和题目二中任这一题作为本章的作业题目、另外的一题可作为达做题。

Question 1 [edt] edt source]

假设在大气晨顶 (TDA) , 在多年全年平均的情况下、入财的太阳辐射随纬度的分布满足 $Q = Q_o \cdot s(x), s(x) = s_o \cdot P_o(x) + s_2 \cdot P_2(x)$ 、其中、 $P_o(x) = 1, P_2(x) = \frac{1}{2}(3x^2 - 1), s_o = 1, s_2 = -0.473, x = sin\phi, \phi$ 为结歴。

如果假设大气层顶的向外净长波辐射为J,行星反照率为cc,且忽略它们随纬度和经度的变化:

1. 请写出在能量平衡的情况下,大气和海洋的总经向能量输送应满足什么条件?

- 2. 按(1)中的条件。大气和海洋的总经向能量输送的最大值应出现在什么纯度?
- 3. 靖与实际情况的大气海洋的能量输送相比较,讨论(2)结果是否与实际状况相符合?

Question 2 [edit|edit source]

在第二章中,我们学习了Budyko的能量平衡气候模型(Simple Energy Balance Climate Model),并用此模型来讨论了存在冰雪线的情况下,气候系统的 稳定性问题,冰雪线的南北移动会引起行星反照率及热量的动力输送的变化,我们发现这两种过程的相互作用能够引起气候系统的不稳定。如果使用同样 的参数,即 $A = 211.1W/m^2$, $B = 1.55W/(m^{2*}C)$, $Q_{\nu} = 340W/m^2$, $T_{max} = -10^{\circ}C$, $s(x) = 1 - 0.241(3x^2 - 1)$, 并同样假没:

$$\mathcal{A}(T) = egin{cases} lpha & T < T_{ ext{slow}}, \ eta & T > T_{ ext{slow}}, \ lpha & T > T_{ ext{slow}}, \ rac{lpha+eta}{2} & T = T_{ ext{slow}}. \end{cases}$$

如果行星反照率发生了改变,使得α = 0.43。 请讨论:

1. 为了保持全球平均温度了不安,对于当前的Q和冰雪线, //应该取多少?

2. 对于新的 α 和 β 值, C的取值应该为多少?

3. 请计算出新的 $Q(x_{s})$.

4. 请与课堂上所讲的 $\alpha = 0.4, \beta = 0.7$ 的情况相比较(请将两种情况下 $Q(x_s)$ 的由线画在同一张图上),讨论两种情况的异同,尤其是气候稳定性 在 α 和 β 值改变后发生了何种变化,请讨论为什么会发生这些变化?

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